

# SUPERCONTINUUM GENERATION USING ELLIPTICAL SILICON CORE PHOTONIC CRYSTAL FIBER

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## ABSTRACT

A new design of elliptical solid core photonic crystal fiber (PCF) is proposed using COMSOL Multiphysics software based on finite element method. The cross section of the PCF is modeled with circular airholes and an elliptical core made of silicon. Results for the effective refractive index, dispersion properties of the PCF, Effective mode area and Nonlinearity are presented. For Supercontinuum (SC) generation higher order dispersion terms and nonlinear coefficient of the PCF are calculated. Numerical simulation of SC generation for the proposed PCF is analysed using the generalized nonlinear Schrodinger equation and split step Fourier transform method. The SC generation of about 300nm is observed when the input pulse of femtosecond duration is pumped in the anomalous dispersion regime of the fiber.

**Keywords :** Dispersion (D), effective refractive index ( $N_{eff}$ ), effective area ( $A_{eff}$ ), Photonic Crystal fiber (PCF), super continuum (SC).

## 1. INTRODUCTION

Photonic crystal is a periodic nanostructure that affects the motion of photons in the same way that ionic lattices affect electrons in solids. Photonic crystal fibers are being increasingly used in the place of optical fibers they consist of a periodic array of air holes running along the entire fiber length. There are two main light guiding mechanisms in PCF. The first one is Index guiding fibers that have a solid core and guides light through total internal reflection like conventional fibers. On the other hand, the second one is hollow core PCF which transmits light by photonic bandgap effect. PCF provides enhanced design flexibility compared to standard optical fibers by changing the size and distance between the air holes [1]. PCFs have attracted significant attention because of their unique optical properties such as endlessly single mode operation [2], adjustable dispersion [3], anomalous group-velocity dispersion at visible wavelength [4,5], high birefringence [6], high or low nonlinearity, low confinement loss, etc. The combination of the unique dispersion properties and enhanced nonlinearities can be used to obtain Supercontinuum (SC) generation when the fiber is pumped with short pulses of laser light

with wavelength near the zero-dispersion wavelength (ZDW) [7]. Supercontinuum (SC) generation occurs when a high power ultrashort optical pulse propagates through a nonlinear optical medium and undergoes extreme nonlinear spectral broadening to yield a broadband spectrally continuous output. The SC characteristics depend particularly on the position of the input pulse wavelength relative to the fiber ZDW [8]. SC is an attractive coherent source for optical coherence tomography, spectroscopy and optical frequency metrology [9]. In this paper, a PCF is designed using COMSOL Multiphysics and the refractive index and dispersion property are calculated. The higher order dispersion parameters and nonlinear coefficient of the proposed PCF is used for the numerical simulation of SC generation using Generalized Nonlinear Schrödinger equation (GNLSE). To solve the GNLSE we have used the split step Fourier transform method. In the anomalous dispersion regime of the fiber the dispersion parameter  $\beta_2$  is less than zero and fiber can support solitons. The SC generation is observed when the input pulse of femtosecond duration is pumped in the anomalous dispersion regime of the fiber.

## II. PCF DESIGN

A solid core PCF consists of a periodic array of air-holes with a central defect acting as the core and the optical parameters of the fiber is determined by the pitch ( $\Lambda$ ) 1.4  $\mu\text{m}$  and diameter ( $d$ ) 1.1  $\mu\text{m}$  of the air holes. And the PCF has a central air core in the form of an ellipse as ellipse has the least confinement loss compared to other structures of major axis 1.5  $\mu\text{m}$  and minor axis 0.3  $\mu\text{m}$ . The diameter of the inner ring air holes is reduced to 0.84  $\mu\text{m}$  to provide better confinement. The geometry of the PCF used was a hexagonal pattern with a periodic triangular lattice arrangement of airholes as shown in Fig.1.

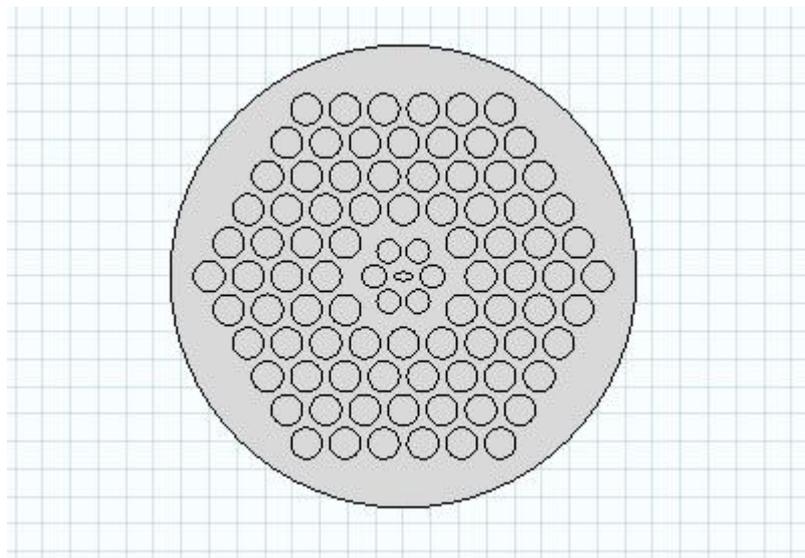


Fig 1 : Geometry of Hexagonal PCF with elliptical core

The material used for the PCF is silica and the elliptical core is made up of silicon. The refractive index of the material is determined using Sellmeyer's equation, while the index of air is constant ( $n=1$ ). Fig 2 shows the field plot of time average power flow in z direction at wavelength  $\lambda=1000$  nm. It can be observed that the light is well

confined to the core region and penetrates only slightly into the cladding region and in the shorter wavelength the light will be more confined in the core part.

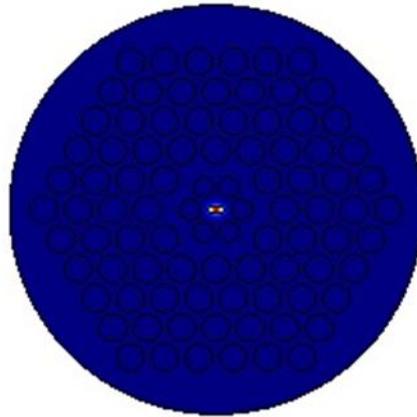


Fig 2 : Mode field distribution at  $\lambda=1000\text{nm}$

From COMSOL we get the values of effective mode index ( $n_{\text{eff}}$ ) for different values of wavelength. Fig.3 shows the variation of effective refractive index as a function of wavelength for the PCF. It is important to calculate the effective index of a fiber accurately as waveguide dispersion is related to the second order derivative of effective index with respect to wavelength. From figure 3, it is noted that the effective index of refraction decreases with the increase in wavelength.

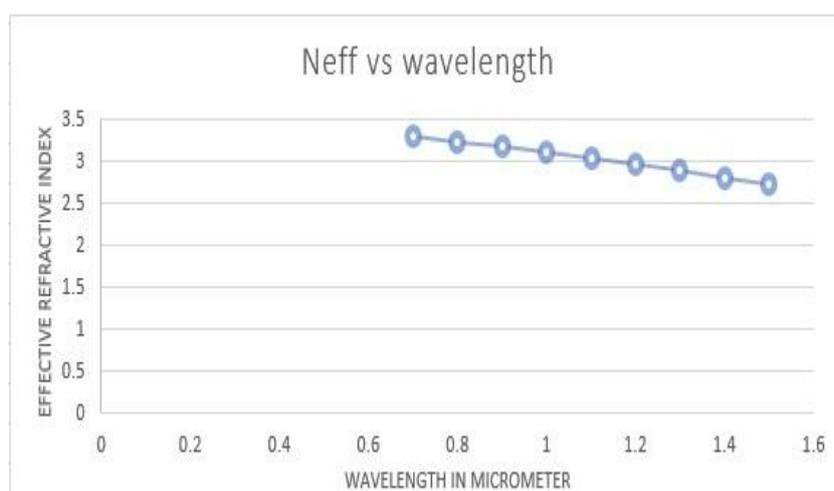


Fig 3: Effective refractive index Vs Wavelength plot

By using the effective refractive index waveguide dispersion  $D$ , is calculated from the following equation ,

$$D(\lambda) = -\frac{\lambda}{c} \frac{d^2 \text{Re}[N_{\text{eff}}]}{d\lambda^2} \quad (1)$$

where  $N_{\text{eff}}$  is the effective refractive index of the guided mode,  $\lambda$  is the wavelength, and  $c$  is the velocity of light in vacuum. Fig.4 shows the dispersion characteristics of the PCF as a function of wavelength.

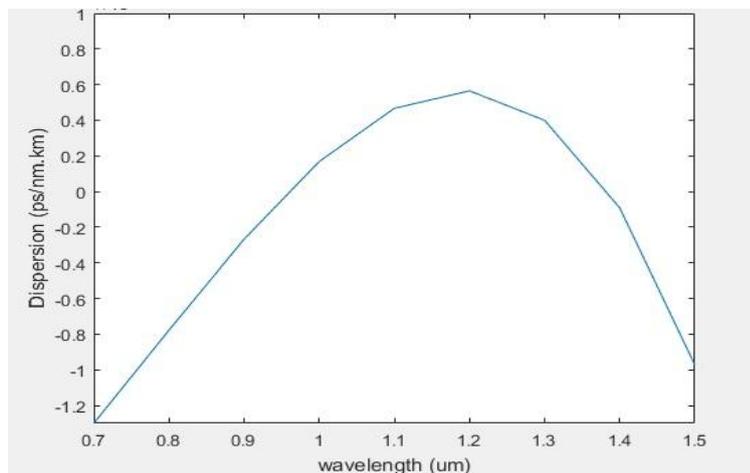


Fig 4: Dispersion of PCF Vs Wavelength

Fiber Nonlinearity is calculated using the formula,

$$\gamma = \frac{n_2 \omega_0}{c A_{\text{eff}}} \quad (2)$$

Where  $n_2$  for silicon is  $4.5 \times 10^{-18} \text{ m}^2/\text{W}$ ,  $c$  is the speed of light,  $A_{\text{eff}}$  is the effective mode area,  $\omega_0$  is the centre frequency. Fibers with high  $\gamma$  values are attractive for a broad range of applications in nonlinear fiber devices. It is evident that the effective nonlinearity  $\gamma$ , decreases as the wavelength increases as in fig 6. This is due to the fact that the mode area becomes larger at higher wavelengths. For lower wavelengths, the small core diameters exhibit strong nonlinearity due to the strong mode confinement.

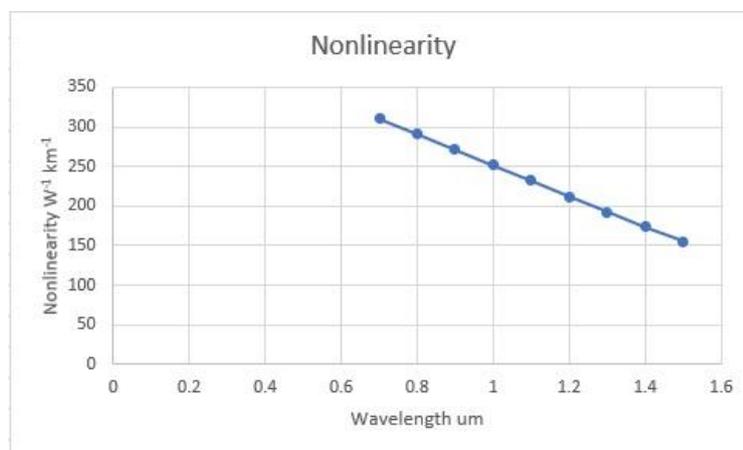


Fig 5: Nonlinearity of PCF vs wavelength

The higher order dispersion coefficients are given by the following equation,

$$\beta_m = \frac{\partial_m \beta}{\partial \omega^m} \quad (3)$$

Where  $m=2,3,4$  represents the  $m^{\text{th}}$  order of dispersion coefficient,  $\beta$  is the mode propagation constant,  $n$  is the refractive index,  $\omega$  is the angular frequency and  $m$  the degree of the derivative. The parameters  $\beta_1$  and  $\beta_2$  are calculated by the relations,

$$\beta_1 = d\beta/d\omega \quad (4)$$

$$\beta_2 = d\beta_1/d\omega \quad (5)$$

Where  $\beta_2$  represents the group velocity dispersion. The Proposed PCF has two wavelengths at which the dispersion is zero, 0.961 $\mu\text{m}$  and 1.381 $\mu\text{m}$ . The higher-order dispersion parameters and the nonlinear coefficient at wavelength 1000 nm are calculated and are shown in Table.1.

$\beta_2$	-3.9462
$\beta_3$	5.8787e-3
$\gamma$	251.9W <sup>-1</sup> Km <sup>-1</sup>

TABLE 1 : Parameters for the Proposed PCF at 1000nm

The propagation of pulse in an optical fiber is described by the generalized nonlinear Schrodinger equation (GNLSE)

$$\frac{\partial}{\partial z} A(z, t) = -\frac{\alpha}{2} A(z, t) + \sum_{m \geq 2} \beta_m \frac{i^{m+1}}{m!} \frac{\partial^m}{\partial t^m} A(z, t) + i\gamma \left( 1 + \frac{i}{\omega_0} \frac{\partial}{\partial t} \right) [A(z, t) \int_{-\infty}^{+\infty} R(t') |A(z, t - t')|^2 dt'] \quad (6)$$

where  $A(z, T)$  is the electric field envelope in a retarded time frame  $T=t-\beta_1 z$ . Non-linear response  $R(t)$  can be defined as

$$R(T) = (1-f_R)\delta(T) + f_R h_R(\tau) \quad (7)$$

$$h_R(t) = \frac{\tau_1 + \tau_2}{\tau_1 \tau_2} \exp\left(-\frac{t}{\tau_2}\right) \sin\left(\frac{t}{\tau_1}\right) \quad (8)$$

Where  $f_R = 0.43$  is the fractional contribution of the Raman response and  $h_R(t)$  is the Raman response function with Raman period ( $\tau_1 = 0.01\text{ps}$ ) and lifetime ( $\tau_2 = 3\text{ps}$ ).

The GNLSE equation (6) is a nonlinear partial differential equation that does not have known analytical solution. Therefore a numerical approach is often necessary for an understanding of the nonlinear effects in fibers. We used the split step Fourier method to solve the GNLSE.

### III. SIMULATION RESULTS

Numerical simulation for SC generation process using femtosecond pulse taken in the anomalous dispersion regime of the proposed PCF using equation (6) is presented. We consider the length of the PCF to be 0.01m. The initial input pulse used in the simulation is a hyperbolic secant pulse, where  $T_0 = 20$  fs, peak power  $P_0 = 25$  W at 1000 nm wavelength. The input pulse is pumped in the anomalous dispersion regime of the PCF where fibers support solitons. A broad spectrum of nearly 300nm is obtained, SC generation involves various processes including the soliton breakup, self-phase modulation, self-steepening effect, intrapulse Raman Scattering, and dispersive wave generation due to higher-order dispersion. The soliton undergoes the fission process and breaks up into a series of lower amplitude pulses because of the perturbations caused by the higher order dispersion and nonlinear effects.

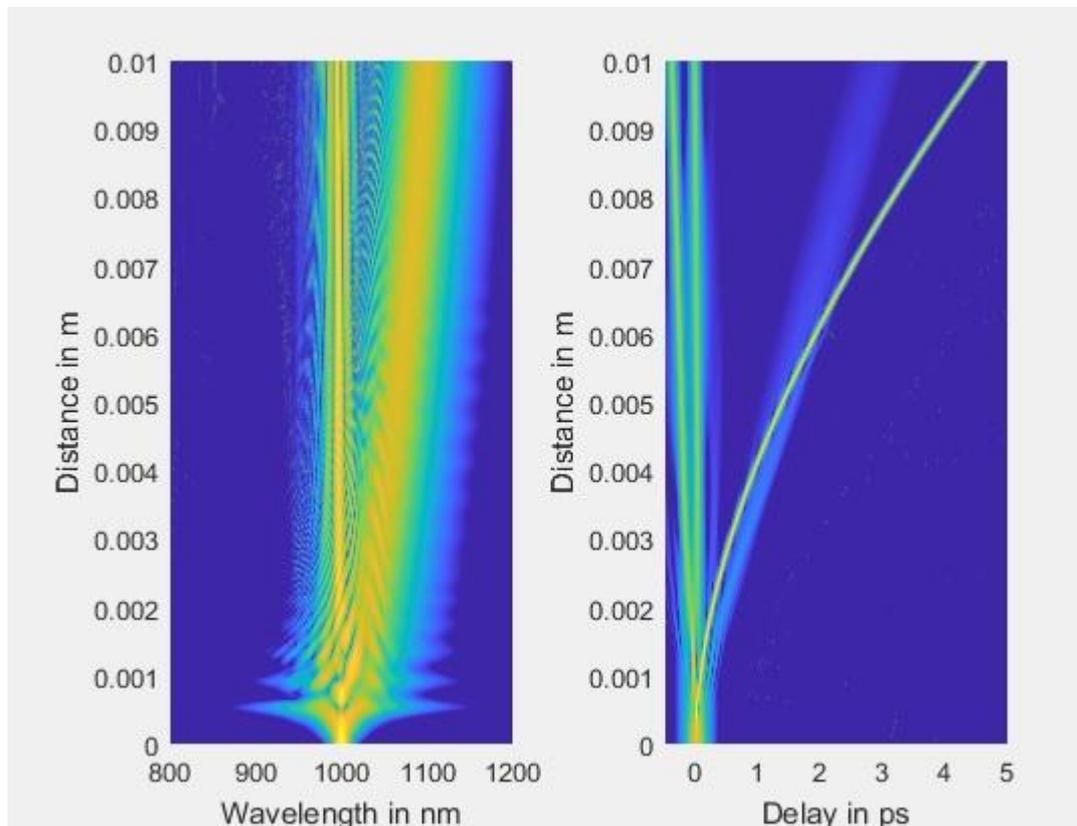


Fig 6: Supercontinuum Generation for the Elliptical core PCF

### IV. CONCLUSION

We have designed the Elliptical Silicon core photonic crystal fiber with circular air holes for Supercontinuum generation using COMSOL. The zero dispersion wavelength of the fiber was 961 nm and 1381 nm and the dispersion slope agrees with the published numerical result. For SC generation the input pulse is pumped in the anomalous dispersion regime of the PCF and the result of the higher order dispersion parameters and nonlinear coefficient of the PCF at wavelength 1000 nm are presented. The SC generation is observed using the

proposed PCF of length 0.01 m and the spectrum of SC extends to about 300 nm, which can be used for various applications such as Optical coherence Tomography etc.

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