



AREA AND POWER EFFICIENT CARRY SELECT ADDER USING BRENT KUNG ARCHITECTURE

S.Durgadevi¹, Dr.S.Anbukarupusamy², Dr.N.Nandagopal³

Department of Electronics and Communication Engineering

Excel Engineering College, Komarapalayam, Namakkal-637303, Tamilnadu, (India)

ABSTRACT

Carry Select Adder (CSA) architectures are proposed using parallel prefix adders. Instead of using dual Ripple Carry Adders (RCA), parallel prefix adder Brent Kung (BK) adder is used to design Regular Linear CSA. Adders are the basic building blocks in digital integrated circuit based designs. They work by creating two signals for each bit position, based on whether a carry is propagated through from a less significant bit position, generated in that bit position, or killed in that bit position. Carry Select Adder is a compromise between RCA and CLA in term of area and delay. Delay of RCA is large therefore we have replaced it with parallel prefix adder which gives fast results. In this system, structures of 16-Bit Regular Linear Brent Kung CSA, Modified Linear BK CSA, Regular Square Root (SQRT) BK CSA and Modified SQRT BK CSA are designed. Power and delay of all these adder architectures are calculated at different input voltages.

Keywords-CSA RCA BK CLA (SORT).

I. INTRODUCTION

Very large scale integration (VLSI) is the process of creating an integrated circuit (IC), combining thousands of transistors into a single chip. The strict limitation on power dissipation in any device must be met by the VLSI chip designer without compromising in their computational requirements[1]. Reducing the total power consumption in such system is important since it is desirable to maximize the run time with minimum requirements on size, battery life and weight allocated to batteries. So the most important factor to consider while designing any circuit is 'low power'.

The term Prefix means, the outcome of the operation depends on the initial inputs. Parallel adders involve the execution of an operation in parallel. This is done by segmentation into smaller pieces that are computed in parallel[2]. It is fast because the processing is accomplished in a parallel fashion. The Operation can be any arbitrary primitive operator that is associative is parallelizable.

II. ADDERS

The most basic arithmetic operation that digital computers can perform is addition of binary digits. In electronics, an adder or summer is a digital circuit that performs addition of numbers and is a fundamental building block in VLSI[3]. Adders are used not only in the arithmetic logic units but also in digital signal processor or any other kind of processors are used to calculate addresses and table indices. Although adders can be constructed for many numerical representations such as binary coded decimal or excess code, the most common adders operate on binary numbers also in cases where two's complement or other complement is being used to represent negative numbers.

III. TYPES OF ADDERS

Adders can be broadly classified into two major categories namely,

- Serial Adders
- Parallel Adders.

IV. SERIAL ADDER

A serial adder is used to add binary numbers in serial form. The two binary numbers to be added serially are stored in two shift registers. Bits are added one pair at a time through a single full adder. Serial addition is done by a flip-flop and a full adder. The carry out of the full adder is transferred to a D flip-flop. The output of this flip-flop is then used as the carry input for the next pair of significant bits. The sum bits from the S output of the full adder could transfer to a third shift register. By shifting the sum into a while the bits of A are shifted out, it is possible to use one register for storing both augends and sum of the bits. The serial input register b can be used to transfer a new binary number. The addend bits are shifted out during the addition.

V. PARALLEL ADDER

A binary parallel adder is a digital circuit that adds two binary numbers in parallel form and produces the arithmetic sum of those numbers in parallel form. The full adder is connected in a chain. The output carry from each full adder is connected to the input carry of the next full adder in the chain. The parallel adder is classified into ripple carry adder, carry look-ahead adder[4].

5.1 Ripple Carry Adder (RCA)

A RCA is simply several full adders connected in a series so that the carry must propagate through every full adder before addition is complete. RCA requires the least amount of hardware of all adders, but they are the slowest.

Show fig1.4.1(a)

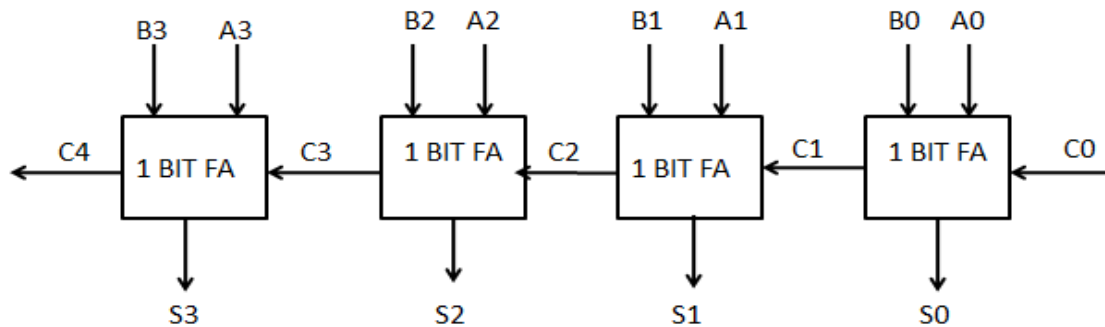


Fig.1.4.1(a) Block Diagram Of Ripple Carry Adder (RCA)

The interconnection of four full adder circuits provides a 4-bit parallel adder. The augend bits of ‘A’ and addend bits of ‘B’ are designated by subscript numbers from right to left, with subscript 1 denoting the lower order bit. The carries are connected in a chain through the full adders. The input carry to the adder is C_{in} and the output carry is C_o. The S outputs generate the required sum bits. When the 4-bit full adder circuit is enclosed within an IC package, it has four terminals for augend bits, four terminals for the addend bits, four terminals for the sum bits and two terminals for the input and output carries. An n-bit parallel adder requires n full adder. The output carry from one packages must be connected to the input carry of the one with the next higher-order bits the 4-bits full adder.

The 4-bit parallel adder in figure 1.1(a) sum (S₁) and carry out (C₁) bits given by full adder 1 are not valid, until after the propagation delay of full adder1. Similarly, the sum S₂ and carry out(C₂)bits given by full adder2 are not valid until after the cumulative propagation delay of two adder, and so on.

At each stage, the sum bit is not valid until after the carry bits in all the preceding stages are valid in effect, carry bits must propagate or ripple carry through all stages before the most significant sum bit is valid. Thus, the total sum the parallel output is not valid after the cumulative delay of all the adders. The sum and carry-out of the adder can be calculated as,

$$\text{Sum} = A \oplus B \oplus C$$

$$\text{Carry} = (A \& B) \vee (B \& C) \vee (A \& C)$$

$$\text{Propagation delay (RCA)} = (N-1) t_{RCA \text{ carry}} + N.t_{RCA \text{ sum}}$$

Where,

t_{RCA carry} - the delay for the carryout

t_{RCA sum} - the delay for the sum

The parallel adder in which the carry out of each full adder is the carry-in to the next most significant adder is called RCA[6]. The greater the numbers or bits that a ripple carry adder must add, the greater the time required for it to perform a valid addition. If two numbers are added such that no carries occur between stages then the add time is simply the propagation time through a single full adder. RCA is faster than serial adder and low power consumption. The drawback of RCA is very slow.

5.2 Carry Look Ahead Adder (CLA)

A CLA is a type of adder used in digital logic .A CLA improves speed by reducing the amount of time required to determine carry bits.

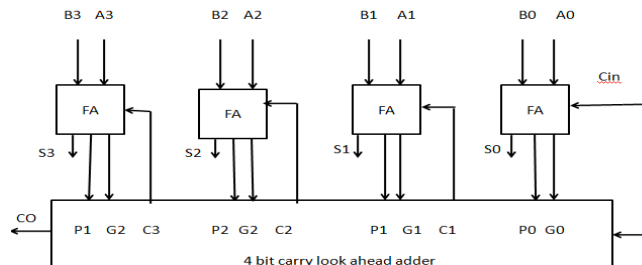


Fig .1.4.2(B)Block Diagram Of Carry Look Ahead Adder (CLA)

Carry look-ahead logic uses the concepts of generating and propagating carries. Although in the context of a carry look-ahead adder, it is most natural to think of generating and propagating in the context of binary addition, the concepts can be used more generally than this. In the descriptions below, the word digit can be replaced by bit when referring to binary addition.

The addition of two 1-digit inputs a and b is said to generate if the addition will always carry, regardless of whether there is an input carry equivalently, regardless of whether any less significant digits in the sum carry.

For example, in the decimal addition $52 + 67$, the addition of the tens digits 5 and 6 generates because the result carries to the hundreds digit regardless of whether the ones digit carries. The delay is linearly dependent on N, (length of the adder) and the carryout signal contributes largely to the delay. Circuit level modifications that reduce carryout can greatly speeds up the addition operation .The carryout can be calculated with generate, propagate, and carry in. The signals g and p are not dependent on carry in, and can be calculated as soon as the input operands arrive. Weinberger and smith invented the CLA. The main idea behind CLA addition is to generate all incoming carries in parallel and avoid unnecessary delay for carry propagation from the stage of the adder where it has been generated. Very short carry propagate, that is independent of word length

Carry look ahead depends on two things:

- Calculating, for each digit position, whether that position is going to propagate a carry if one comes in from the right.
- Combining these calculated values to be able to deduce quickly whether, for each group of digits, that group is going to propagate a carry that comes in from the right.

The net effect is that the carries start by propagating slowly through each 4-bit group, just as in a ripple-carry system, but then move 4 times as fast, leaping from one look ahead carry unit to the next[5]. Finally, within each group that receives a carry, the carry propagates slowly within the digits in that group.

The more bits in a group, the more complex the look ahead carry logic becomes, and the more time is spent on the slow roads in each group rather than on the fast road between the groups provided by the look ahead carry logic. On the other hand, the fewer bits there are in a group, the more groups have to be traversed to get from one end of a number to the other, and the less acceleration is obtained as a result.

Deciding the group size to be governed by look ahead carry logic requires a detailed analysis of gate and propagation delays for the particular technology being used.

5.3. Carry Select Adder (CSA)

CSA is particular way to implement an adder in electronics device, which is a logic element that computers the (n+1)-bit sum of two n-bit numbers. The CSA is simple but very

Fast

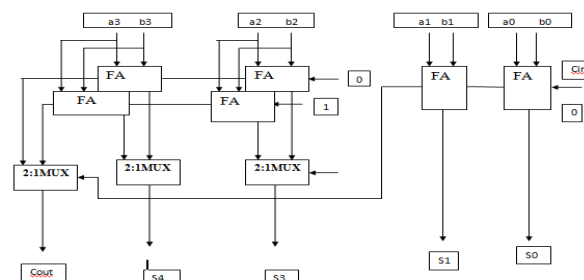


Fig.1.4(c) Block Diagram Of Carry Select Adder (CSLA)

The carry select adder includes in the category of conditional adder. Here sum and carry are calculated by assuming input carry as 0 and 1 separately which are fed to a multiplexer whose select signal is the carry out of previous stage. The conventional carry select consists of $k/2$ bit adder for the upper half most significant bit's (MSB) two k bit adders. This technique of dividing adder into stages increases the area utilization but also speeds up the addition operation. The block diagram of conventional k CSA adder is shown in figure 1.4(c). The CLA is used in many computational systems to alleviate the problem of carry propagation delay by independently generating multiple carries and then select a carry to generate the sum. CLA is parallel computation reduced to carry propagate length and this type adder is very fast calculate all the inputs simultaneously. Draw of CSA is more costly than other adder and designing is complex.

Carry select adder is a particular way to implement an adder, which is a logic element that computes the (n+1)-bit sum of two n -bit numbers. The carry-select adder is simple but rather fast, having a gate level depth of (n).

The carry-select adder generally consists of two ripple carry adders and a multiplexer. Adding two n -bit numbers with a carry-select adder is done with two adders therefore two ripple carry adders in order to perform the calculation twice, one time with the assumption of the carry being zero and the other assuming one. After the two results are calculated, the correct sum, as well as the correct carry, is then selected with the multiplexer once the correct carry is known.

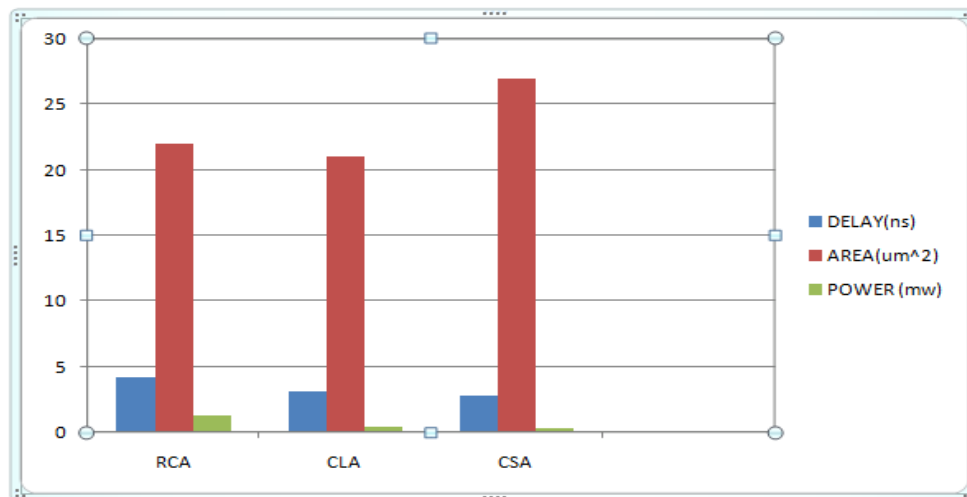
The number of bits in each carry select block can be uniform, or variable. In the uniform case, the optimal delay occurs for a block size. When variable, the block size should have a delay, from addition inputs A and B to the carry out, equal to that of the multiplexer chain leading into it, so that the carry out is calculated just in time. The delay is derived from uniform sizing, where the ideal number of full-adder elements per block is equal to the square root of the number of bits being added, since that will yield an equal number of MUX delays.



A conditional sum adders a recursive structure based on the carry-select adder. In the conditional sum adder, the MUX level chooses between two bit inputs that are themselves built as conditional-sum adder[7]. The bottom level of the tree consists of pairs of 2-bit adders (1 half adder and 3 full adders) plus 2 single-bit multiplexers.

PARAMETERS	DELAY ns	AREA μm^2	POWER mw
RCA	4.208 (Very high)	2214 (Less)	0.261 (Low)
CLA	3.12 (Much less)	2793 (High)	0.261 (Much high)
CSA	2.81 (Less)	2160 (Much less)	0.312 (High)

1.4.(D) Comparison Of Parameter Adder



1.4.(E) Bar Chart Of Parameter Adder

VI. 16-BIT LINEAR MODIFIED BK CSA

Regular Linear Brent Kung Carry Select Adder uses single Ripple Carry Adder (RCA) for $C_{in}=0$ and Brent Kung adder[8] for $C_{in}=1$ and is therefore area-consuming. So, different add-one schemes like Binary to Excess-1 Converter (BEC) have been introduced. Using BEC, Regular Linear BK CSA is modified in order to obtain a reduced area and power consumption. Binary to Excess-1 converter is used to add 1 to the input numbers[9]. So, here Brent Kung adder with $C_{in}=1$ will be replaced by BEC because it require less number of logic gate for its implementation so the area of circuit is less. Linear Modified BK CSA is designed using Brent Kung adder for $C_{in}=0$ and Binary to Excess-1 Converter for $C_{in}=1$ in order to reduce the area and power consumption with small speed penalty. Linear Modified BK CSA consists of 4 groups.

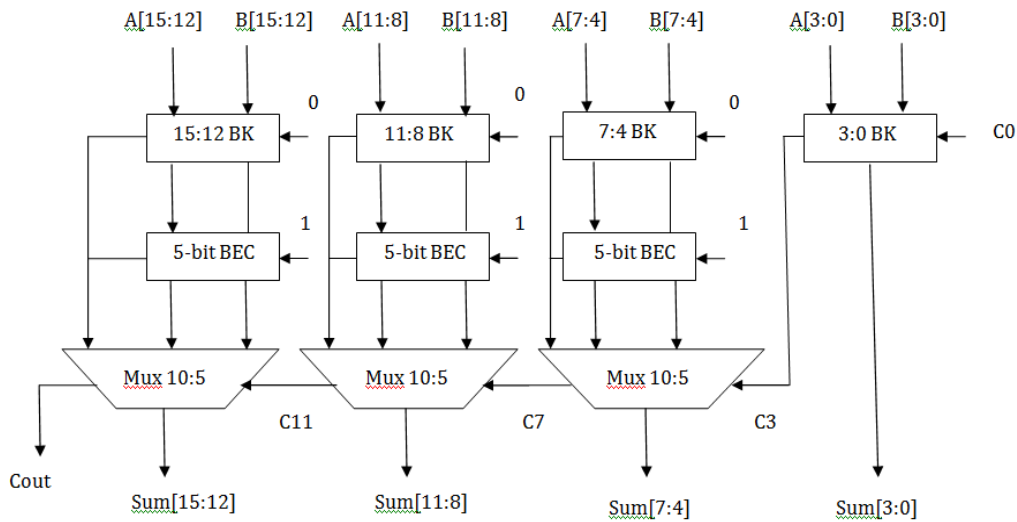


Fig 4.1(a) Block Diagram Of 16-Bit Linear Modified BK CSA

To replace the N-bit Brent Kung adder, aN+1 bit BEC is required. The importance of BEC logic comes from the large silicon area reduction when designing Linear Modified BK CSA for large number of bits.

VII. REGULAR SQUARE ROOT BRENT KUNG CARRY SELECT ADDER

Regular Linear Brent Kung Carry Select Adder consumes large area and to reduce its area a new design of adder is used i.e. Regular Square Root Brent Kung Carry Select Adder. Regular Square Root BK CSA has 5 groups of different size RCA for Cin=1 and MUX. High area usage and high time delay are the two main disadvantages of Linear Carry Select Adder. These disadvantages of linear carry select adder can be rectified by SQRT CSA. It is an improved version of linear CSA. The time delay of the linear adder can decrease, by having one more input into each set of adders than in the previous set. This is called a Square Root Carry Select Adder[2].

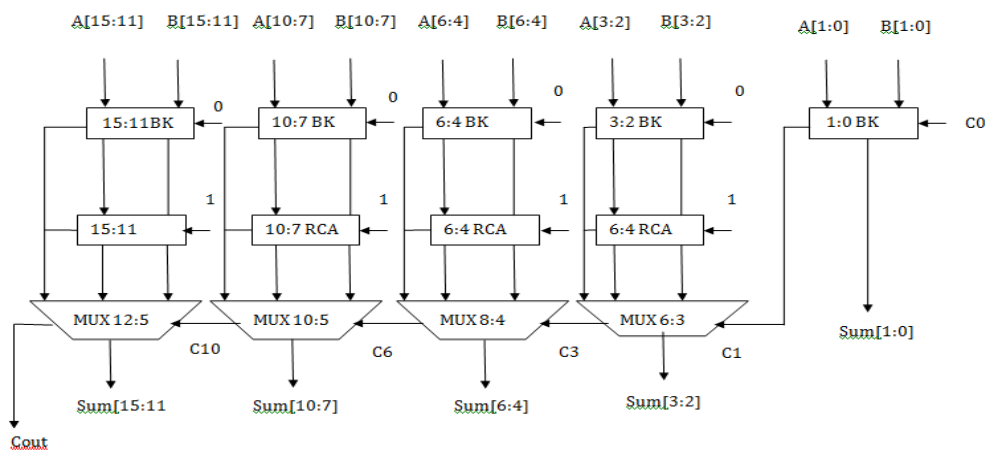


Figure 4.2 (a) Regular Square Root Brent Kung Carry Select Adder



VII. MODIFIED SQUARE ROOT BRENT KUNG CARRY SELECT ADDER

Modified Square Root Brent Kung Carry Select Adder has been designed using Brent Kung adder for $C_{in}=0$ and BEC for $C_{in}=1$ and then there is a multiplexer stage. It has 5 groups of different size Brent Kung adder and Binary to Excess-1 Converter (BEC). BEC is used to add 1 to the input numbers. Less number of logic gates are used to design BEC as compared to RCA therefore it consumes less area.

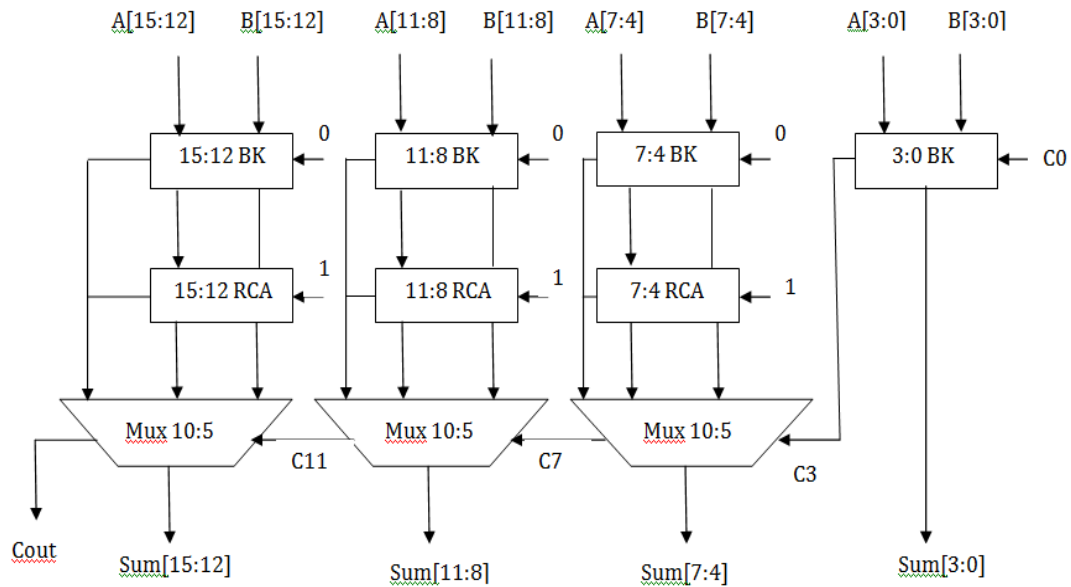


Figure 4.4(a) Regular Linear Brent Kung Carry Select Adder

Binary excess converter:



By giving 4 inputs (B0 B1 B2 B3) the outputs obtained are (X0 X1 X2 X3) here we use 2 wire lines and for an inputs of 7 we get an output 8 that is the output exceeds input by the value of 1.

10:5 Mux:

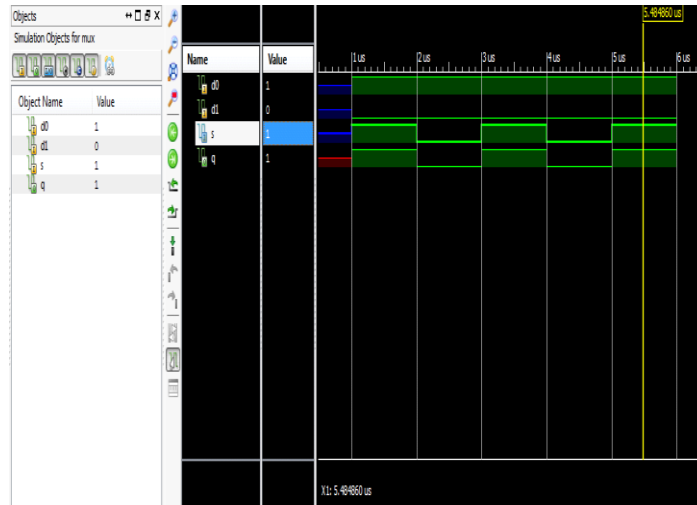


Figure 4.6(a) 10:5 Mux (Output)

In multiplexer we will give 2 inputs (do, d1) and there will be an single output (q).we will use single selection line whose when it is 0^{1st} output will be displayed when it is 1 the another one will be displayed

Brent Kung adder:

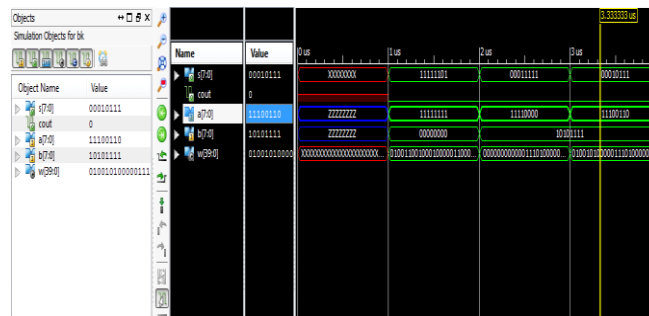
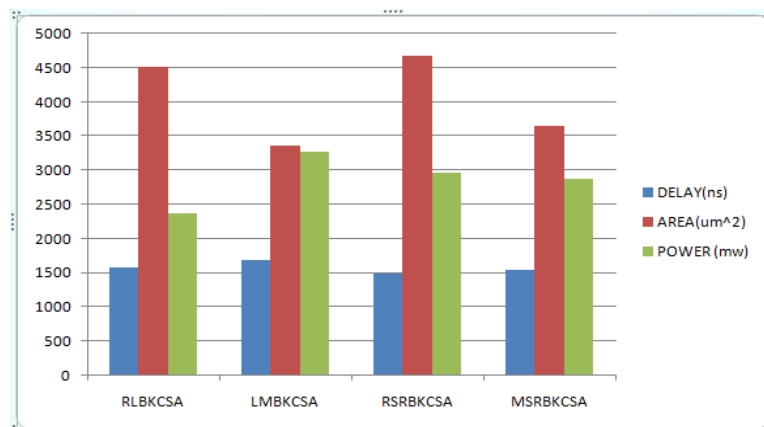


Figure 4.7 (a) Brent Kung adder (output)

In this there will be 8 inputs (a [0:7], [0:7] b) and equal number of outputs. We use 37 wires in this. To produce the output we will use generate and propagate operations[8].

ADDERS	AREA (ns)	POWER (mw)	DELAY (um ²)
Regular linear BK CSA	4516	182375.81	1588
Linear Modified BK CSA	3364	193367.07	1688
Regular Square Root BK CSA	4676	81296.89	1485
Modified Square Root BK CSA	3655	89885.90	1550

4.8 Comparisons of parallel prefix adder:



4.9 Bar Chart Comparisons of parallel prefix adder

VIII. CONCLUSION

In this work, a Modified Square Root BK Carry Select Adder is proposed which is designed using single Brent kung adder and Binary to Excess-1 Converter instead of using single Brent kung adder for $C_{in}=0$ and Ripple Carry Adder for $C_{in}=1$ in order to reduce the delay and power consumption of the circuit. Here, the adder architectures like Regular Linear BK CSA, Modified Linear BK CSA, Regular SQRT BK CSA and Modified SQRT BK CSA are designed for 16-Bit wordsize only. This work can be extended for higher number of bits also. By using parallel prefix adder, delay and power consumption of different adder architectures is reduced.

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