ISSN-2319-8354(E)

# COMPARATIVE ANALYSIS OF BOW-TIE AND DIPOLE NANOANTENNAS

# Manpreet Singh<sup>1</sup>, Parminder Luthra<sup>2</sup>

<sup>1</sup> P.G Student, Department of Nanotechnology, BMSCE, Muktsar, Punjab, (India) <sup>2</sup> A.P, Department of Nanotechnology, BMSCE, Muktsar, Punjab, (India)

#### **ABSTRACT**

In this paper, Bow-tie and Dipole nanoantennas are presented for infrared & laser communication. The optical characteristics of these nanoantennas are investigated in depth by using the Green's Tensor Technique. Here the effects of geometrical parameters on the antenna's spectral response and field enhancements are presented. Bow-tie & Dipole antennas confine the field in a volume lower than the diffraction limit, defined by the gap dimensions. It is observed that the dipole antenna produces a stronger field enhancement as compared to Bow-tie antenna for all investigated antenna geometries. Dipole can offer high field enhancement of three order of the magnitude for the smallest gap width. Dipole antenna is monomode in the considered spectral range, where as the Bow-tie antenna offers multiple resonances. Instead of these, the sensitivity of these antennas to index changes of the environment and of the substrate is analyzed in depth for Bio-electric Sensor applications. Bow-tie antenna offers slightly higher sensitivity as compared to Dipole antenna.

Keywords: Metal optics, Nanostructures, Optical resonators, Sub-wavelength structures, Surface plasmons.

# I. INTRODUCTION

Over the last 10 years there has been a surge of research in the optical properties of metallic nano-particles. Properly designed nanostructures are known to produce so called hot spots where the incident electromagnetic field is enhanced by several orders of magnitude. The plasmonic resonances observed in such structures open the possibility to build antennas operating in the visible light region of the spectrum. Their hot spots can be used to trigger nonlinear effects and to couple electromagnetic radiation efficiently between the antennas and dipole emitters. Experimental techniques such as tip enhanced Raman spectroscopy or surface enhanced Raman spectroscopy demonstrate the potential of such hot spots to detect radiative emitters with sensitivity down to a single molecule. The enhancement of the fluorescence of molecules placed near a plasmonic nano-structure has been observed recently, tuning the Plasmon resonance either to the excitation or the emission of the molecules.

ISSN-2319-8354(E)

The optical properties of different types of antennas have been discussed over the last few years. Two geometries, i.e. the Dipole and the Bow-tie antennas, appear to combine in a unique way the formation of a strong hot spot in their gap and the tunability of their resonance. The strong field enhancement of dipole antennas has readily been shown by white light continuum generation.

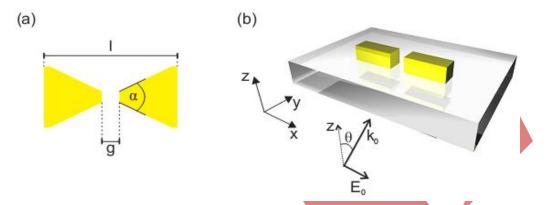


Fig. 1. Geometry of the investigated system: (a) Bow-tie antenna (b) Dipole antenna.

Bowtie antennas have recently been used as near-field probes and for nano-lithography. The potential of both structures for the enhancement of the fluorescence of molecules has also been demonstrated. However a detailed analysis and comparison of the optical properties of both antenna structures as a function of their different geometrical parameters is still not included in the literature. The aim of my paper is to provide such a detailed comparative analysis. The paper is organized as follows: Section II describes the Geometrical model used; the response of Bow-tie and Dipole antennas is discussed in Section III and a conclusion is presented in the IV section.

### II. GEOMETRY & ANTENNA MODELLING

The Green's tensor method is used to calculate the optical response of gold dipole and bowtie antennas. The real and imaginary parts of the gold dielectric function are obtained from experimental data. To account for a realistic environment the antennas are supported by a substrate with index of refraction ns and covered with a material with index  $n_{env}$ . It is essential to consider such environment material for applications in Bio-electric sensing, where the antenna might be immersed in water or another liquid. If not specified otherwise the calculations are performed for a substrate index  $n_{env} = 1.5$  and an environment index  $n_{env} = 1.0$ . The structures are illuminated from below through the substrate, perpendicular to the antenna long axis and at an angle of incidence  $\theta = 70^{\circ}$  to the vertical axis, to fulfill the attenuated total reflection condition at the glass/air interface, as illustrated in Fig. 1(b).

ISSN-2319-8354(E)

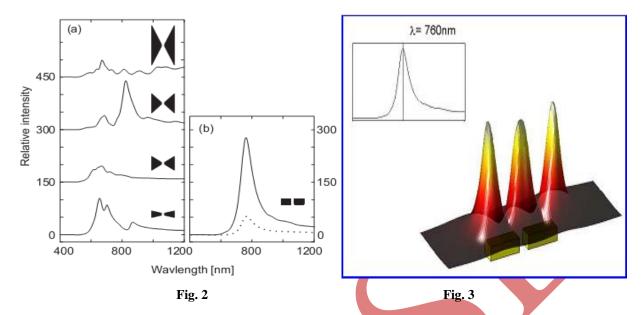


Fig. 2. Relative field intensity spectrum in the gap for (a) Bow-tie and (b) Dipole antennas. The dotted line in window (b) indicates the relative field intensity at the extremity of the dipole antenna. (l = 230 nm; g = 30 nm).

Fig. 3. Near-field intensity distribution 20nm above a dipole antenna (l=230nm) as a function of the illumination wavelength  $\lambda$ . The corresponding spectrum (field intensity in the gap) is shown in the inset.

The incident field E<sub>0</sub> is polarized along the long axis of the antenna as pointed out in the introduction, the gap represents an essential feature of the antenna structure. To characterize the spectral response of the antenna and its intensity enhancement we therefore calculate the field intensity inside this gap in relative units to the illumination intensity I<sub>0</sub> in the substrate. The antennas are divided into 3 meshes of 10x10x10nm size, which leads to the following Bow angles  $\alpha$  for the Bow-tie antenna:  $\alpha_1 = 28^\circ$ ,  $\alpha_2 = 53^\circ$ ,  $\alpha_3 = 90^\circ$  and  $\alpha_4 = 127^\circ$ , Fig. 1(a). All antennas have a 40nm thickness. The width of the dipole antenna is 40nm, whereas the bow-tie antenna apex width is 20nm. These values correspond to what can be achieved with modern fabrication techniques. The mesh used for the calculation provides an accurate description of the antennas. In the next section, we study the spectra of Bow-tie and Dipole antennas as a function of the following geometrical parameters: Antenna length 1, gap width g, substrate index  $n_s$  and environment index  $n_{env}$ , Fig. 1(b).

## III. RESULTS AND DISCUSSION

The geometry of the antenna strongly influences its optical properties as indicated in Figure 2, which shows the calculated intensity spectra in the antenna gap for the dipole antenna and for the Bow-tie antennas with the Bow angles  $\alpha_1$  -  $\alpha_4$ . In the spectral range of the calculation, the dipole antenna has one resonance at 760nm, where the field intensity in the gap is about 280 times larger than the intensity of the illumination field. The Bow-tie antennas produce a lower field in their gaps (about 50-150 times the illumination field intensity).

ISSN-2319-8354(E)

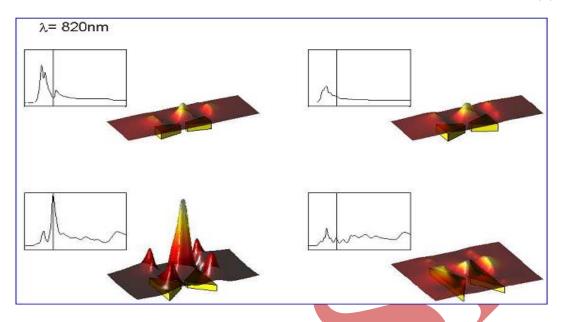


Fig. 4. Near-field intensity distributions 20nm above Bow-tie antennas (l=230nm) as a function of the illumination wavelength  $\lambda$ . Four different Bow angles are considered (from top left to bottom right):  $\alpha 1 = 28^{\circ}$ ,  $\alpha 1 = 53^{\circ}$ ,  $\alpha 1 = 90^{\circ}$  and  $\alpha 4 = 127^{\circ}$ . The corresponding spectra (field intensity in the gap) are shown in the insets.

Figure 2 indicates that the dipole antenna is essentially single mode, while the bowtie antennas exhibit several resonances, whose spectral positions depend on the Bow angle  $\alpha$ . However, a clear trend between Bow angle and field enhancement in the Bow-tie antennas cannot be observed. At the smallest Bow angle  $\alpha$ 1, where the Bow-tie antenna resembles most the dipole antenna, its spectrum approaches most the spectrum of the dipole antenna. The strongest field enhancement is observed for the Bow angle  $\alpha$ 3 = 90° Fig. 2(a). The pattern in Figs. 3 and 4 show the near-field intensity in a parallel plane 20nm above the structure as function of the illumination wavelength.

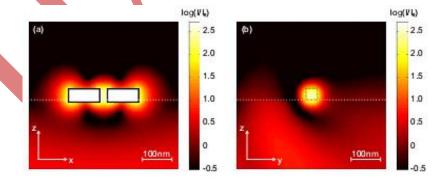


Fig. 5. (a) xz-map and (b) yz-map of the relative field intensity in a plane through the middle of a dipole antenna at the resonance wavelength.

Each resonance corresponds to a specific mode in the near-field. Note that the asymmetry of the near-field along the y axis is due to the inclined illumination. The Bow-tie antennas seem to provide a better localization of the field inside the gap, with less field enhancement at the external edges than observed for the dipole structure. However, the field intensity inside the gap of the dipole structure is larger than for the Bow-tie structures, as can also be seen from the spectra in Fig. 2. The dotted line in Fig. 2(b) represents the intensity at the external edges of the dipole antenna. The intensity in the gap of the dipole antenna is thus about five times larger than at the edges of the antenna. To illustrate the strong field confinement in the antenna gap, Fig. 5 shows the field intensity in the x-z and y-z planes through the gap. The field is confined within a volume of about 40x40x30nm which is well below the limit of diffraction at a wavelength of 760nm. Note the logarithmic scale in the color-plots of Fig. 5. The spectral positions of the antenna resonances are determined by the antenna dimensions. For the chosen incident polarization, the length of the antenna plays the most crucial role. To study this effect further and to simplify the comparison of dipole and bowtie antennas, in the remaining of the paper we will concentrate on the bowtie structure with bow angle  $\alpha_3 = 90^\circ$ , which produces the largest field enhancement. The influence of the antenna length on the resonance spectrum is investigated in Fig. 6.

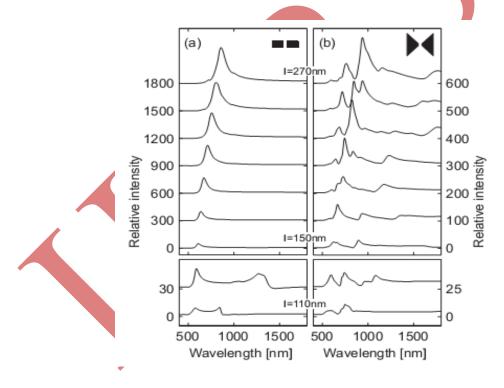


Fig. 6. Relative intensity enhancement in the gap as a function of the antenna length l between l=110nm and l=270nm in 20nm increments. (a) Dipole (b) bowtie geometry ( $\alpha = 90^{\circ}$ ). The antenna gap kept constant (g=30nm).

Note the different intensity scales of the dipole and Bow-tie antennas, as well as the different intensity scales for the short (l=110nm and l=130nm) and for the long antennas, Figs. 6(a) and (b). Two resonances are observed for the

short dipole antennas. In that case, the geometry resembles more that of two coupled nano-particles, supporting two Plasmon modes. The low energy mode shifts very rapidly to the infrared when the structure length increases. Longer dipole antennas ( $l \ge 150$ nm) exhibit one strong resonance which slightly red shifts when the antenna length increases. This effect is investigated in detail in Fig. 7(a), which shows the spectral position of the resonance as a function of the antenna length. For the dipole antenna, the resonance shifts linearly with the antenna length, with a proportion of 2.1 [wave-length/antenna length]. This trend is less obvious for the bowtie antenna, Fig 6(b). While very short antennas show again two peaks, longer bowtie antennas clearly exhibit a multimode behavior with several peaks. Tracking the resonance wavelength of the strongest mode leads to the scattered data in Fig. 7(a). However, by analyzing each resonance individually, one can recover a well defined trend, as indicated in Fig. 8.

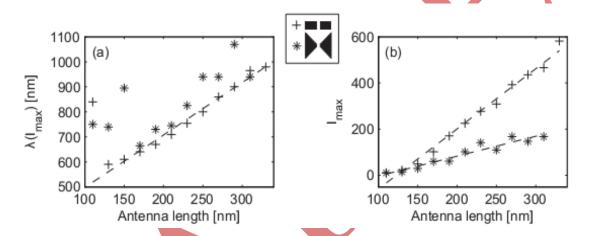


Fig. 7. (a) Resonance position shift for dipole (+) and bowtie ( $\alpha = 90^{\circ}$ , \*) antennas as a function of the antenna length. (b) Field enhancement as a function of the antenna length for both antennas.

The three main resonances identified in Fig. 8(a) for antenna length of l=210nm shift almost linearly with the antenna length, Fig 8(b). The coefficients (between 1.8 and 2.5 [wavelength/antenna length], depending on the resonance Fig. 8(b)) are comparable to that of dipole antenna. Figure 7(b) shows the relative field enhancement in the gap as a function of antenna length. Both antenna types clearly exhibit a linear increase of the field intensity for the range of calculated lengths. The physical origin for this effect is connected to the coupling strength of the two antenna arms. As a matter of fact, the resonance wavelength of a long antenna is larger than that of a short antenna.

Hence, the gap has a smaller effective length for the larger antenna, which results in a stronger coupling between both arms. Note also in Fig. 7(b) that the increase of the field as a function of the antenna length is much stronger for the dipole antenna. However, the increment of the field in the gap of the dipole antenna is much stronger than that of the Bowtie antenna. For the shortest antenna length (110nm) the field is about the same for both structures, whereas for the longest antenna (300nm) the dipole enhancement is about three times higher than the Bowtie enhancement. Stronger field enhancements can be achieved by decreasing the width of the gap. The resulting spectral response is calculated in Figs. 9(a) and (b). Note the logarithmic intensity scale for the color plots.

ISSN-2319-8354(E)

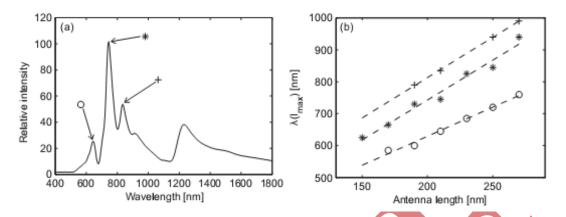
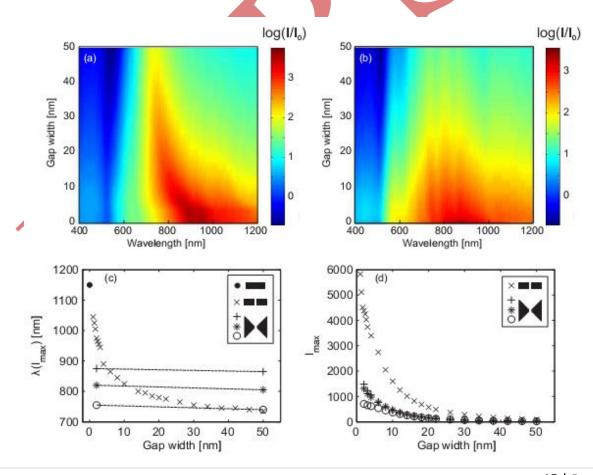


Fig. 8. (a) The three main resonances of a bowtie antenna (l=210nm;  $\alpha = 90^{\circ}$ ) and (b) their spectral position as a function of the antenna length.

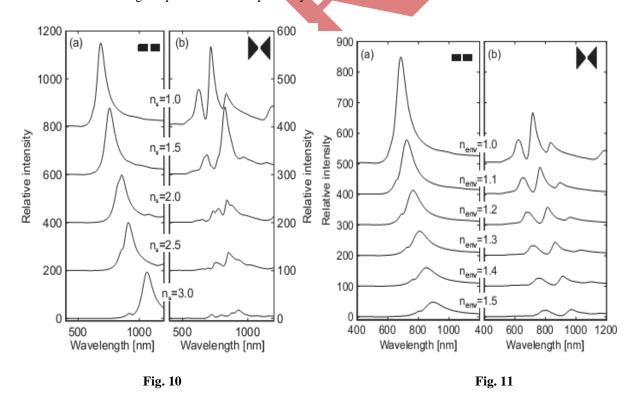
The spectral position of the dipole resonance and of the three main Bowtie resonances as a function of the gap width is shown in Fig. 9(c). For decreasing gap widths the dipole resonance shifts to the red just as observed experimentally for nano-discs by Rechberger et al. On the other hand, the spectral position of the bowtie main resonance remains rather constant.



ISSN-2319-8354(E)

Fig. 9. Relative intensity spectra in the gap as a function of the illumination wavelength and gap width for (a) Dipole and (b) Bowtie ( $\alpha = 90^{\circ}$ ) antenna (l=230nm). (c) Spectral position and (d) relative field enhancement in the gap of corresponding intensity maximum as a function of gap width. For the Bowtie antenna the three main resonances are again treated separately (see Fig. 8).

Both dipole and Bowtie antennas exhibit a strong increase of the field inside the gap for decreasing gap width, as shown in Fig. 9(d). Again this effect is much stronger for the dipole antenna than for the Bowtie antenna. Another interesting effect is visible in Fig. 9(c): For decreasing gap width, the resonance wavelength of the dipole antenna shifts towards that of a monopole antenna with the corresponding length (l=200nm) indicated by a dot in Fig. 9(c). This effect is not observed for the Bowtie antenna. This is probably because in the case of the Bowtie geometry, the structure for touching arms (g=0) is not similar to one individual arm, as is the case for a dipole antenna. Overall, the spectrum of the Bowtie antenna appears to be more determined by the resonance of the two triangular arms, rather than by the coupling between them. At microwave or radio frequencies, the substrate index ns have a strong influence on the resonance spectrum of the antenna. This dependence is in general used to design small antennas with dimensions well below the half wavelength condition. The same effect can be observed in Fig. 10 for optical resonant antennas. An increasing substrate index leads to a red shift of the antenna resonance. At optical frequencies the antenna dimensions are as small as a few tens of nanometers, i.e. below the half wavelength condition and at the limit of today's fabrication techniques. Hence designing smaller antennas by using high index materials as substrate does not seem to be of great practical interest presently.



ISSN-2319-8354(E)

Fig. 10. Relative field intensity enhancement in the gap for (a) Dipole (b) Bowtie antenna (l=110nm, g=30nm,  $\alpha$ =90°) as a function of the illumination wavelength. Different refractive indexes  $n_s$  are used for substrate material.

Fig. 11. Relative field intensity enhancement in the gap for (a) Dipole (b) Bowtie antenna (l=110nm, g=30nm,  $\alpha$ =90°) as a function of the illumination wavelength. Different refractive indexes  $n_{env}$  are used for the cover material, the substrate index is  $n_s$  =1,5.

Much more interesting is the antenna sensitivity to changes of the environmental index of refraction  $n_{env}$  as shown in Fig. 11, the spectral positions of the dipole and the Bowtie resonances strongly depend on  $n_{env}$ . Figure 12(a) and (b) show a linear increase of the resonance wave-length for increasing  $n_{env}$ . Furthermore, the sensitivity of the dipole antenna strongly depends on its gap width: Decreasing the gap width increases the antenna sensitivity as shown in Fig. 12(a). For the bowtie antenna this dependence cannot be observed, Fig. 12(b). All analyzed Bowtie antennas show a slightly higher sensitivity than the dipole antenna (500-510RIU  $^{-1}$  vs. 400-490RIU  $^{-1}$ ).

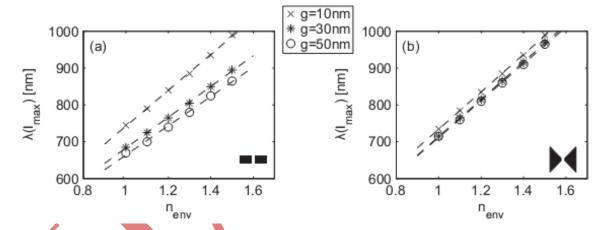


Fig. 12. Sensitivity of the (a) Dipole (b) Bowtie antenna (l=110nm, g=30nm,  $\alpha$ =90°) as a function of the environment index  $\mathbf{n}_{env}$ .

We assume that this sensitivity is related to the spectral position of the antenna resonance. The further the resonance wavelength is shifted to the red, the higher the antenna sensitivity on index changes. Since we have shown previously that the resonance position of the Bowtie antenna remains constant for changing gap widths, the sensitivity to the environment is not changing either for different gaps.

#### IV. CONCLUSION

We have analyzed numerically the optical characteristics of plasmonic Bowtie and Dipole nano-antennas with different bow angles as a function of the antenna length, gap, substrate and back-ground indexes. The Bowtie antenna supports multiple resonances in the examined spectral range, leading to a rather broadband response. The

ISSN-2319-8354(E)

turn out to have similar tuning capabilities with their length. However, the spectral position of the dipole resonance Depends much stronger on the gap width than it is the case for the Bowtie antenna, where almost no spectral shift could be observed. Interestingly the field enhancement is much stronger for the dipole than for the Bowtie antenna. Even though the calculated Bowtie structures have a sharper tip (20nm) than the calculated dipole structures (40nm), the intensity enhancement in the dipole gap reaches values that are three times higher than that of the Bowtie antenna. Despite the stronger field enhancement of the dipole antenna, the bowtie structures show stronger sensitivity to environmental index changes. To the best of our knowledge this is the first detailed comparison of the optical characteristics of Bowtie and dipole antennas. The results of this paper should be useful for choosing the best suited antenna geometry for a given application.

### V. ACKNOWLEDGEMENTS

It is a pleasure to thank Er. Bhupinder Singh for stimulating discussions. Infrastructure backup from the department of Electronics & Communication Engineering, Adesh Institute of Engineering & Technology, Faridkot, Panjab (India).

#### **REFERENCES**

- [1] C. A. Balanis, Antenna theory: analysis and design, 2nd ed. John Wiley and Sons, New York, 1997.
- [2] D. W. Pohl, "Near field Optics seen as an Antennas Problem," in World Scientific, Singapore, pp. 9-21, 2000.
- [3] L. Novotnyand, B.Hecht, Principles of Nano-Optics, chapter 13, Cambridge University Press, 2006.
- [4] E. Cubukcu, et al., "Plasmonic Laser Antennas and Related Devices," *IEEE Journal of selected topics in quantum electronics*, vol. 14, no. 6, pp. 1448-1462, Nov. 2008.
- [5] Q.-H. Park, "Optical antennas and plasmonics," Contemporary Physics, vol. 00, no. 00, pp. 1-20, Jan. 2009.
- [6] P. Bharadwaj, B. Deutsch, and L. Novotny, "Optical Antennas," *Advances in Optics and Photonics*, vol. 1, pp. 438-483, Oct. 2009.
- [7] N. Yu, Q. J. Wang, and M. A. Kats, "Terahertz plasmonics," vol. 1, Dec 2010.
- [8] A. Boltasseve and H. A. Atwater, "Low-loss plasmonic metamaterials," Science,, pp. 290-331, 2011.
- [9] P. Biagioni, J.-S. Huang, and B. Hecht, "Nanoantennas for visible and infrared radiation," *physics optic*, pp. 1-78, Nov. 2011.
- [10] A. E. C. etin, M. Turkmen, S. Aksu, and H. Altug, "Nanoparticle-Based Metamaterials as Multiband Plasmonic Resonator Antennas," *IEEE TRANSACTIONS ON NANOTECHNOLOGY*, vol. 11, no. 1, pp. 208-212, Jan. 2012.
- [11] W. Gotschy, K. Vonmetz, A. Leitner, and F. R. Aussenegg, "Optical dichroism of lithographically designed silver nanoparticle films," *Opt. Lett.* 21, 1099 (1996).
- [12] S. J. Oldenburg, R. D. Averitt, S. L. Westcott, and N. J. Halas, "Nanoengineering of optical resonances," *Chem. Phys.* Lett. 288, 243-247 (1998).

ISSN-2319-8354(E)

- [13] J. Kottmann, O. Martin, D. Smith, and S. Schultz, "Spectral response of plasmon resonant nanoparticles with a non-regular shape," *Optics Express* 6, 213-219 (2000).
- [14] H. Ditlbacher, B. Lamprecht, A. Leitner, and F. R. Aussenegg, "Spectrally coded optical data storage by metal nanoparticles," *Opt. Lett.* 25, 563-565 (2000).
- [15] H. Tamaru, H. Kuwata, H. T. Miyazaki, and K. Miyano, "Resonant light scattering from individual Ag nanopar-ticles and particle pairs," *Appl. Phys.* Lett. 80, 1826-1828 (2002).
- [16] G. Schider, J. R. Krenn, A. Hohenau, H. Ditlbacher, A. Leitner, F. R. Aussenegg, W. L. Schaich, I. Puscasu, B. Monacelli, and G. Boreman, "Plasmon dispersion relation of Au and Ag nanowires," *Phys. Rev.* B 68, 155427 (2003).
- [17] Aizpurua, P. Hanarp, D. S. Sutherland, M. K. all, G. W. Bryant, and F. J. Garc 1a de Abajo, "Optical Properties of Gold Nanorings," *Phys. Rev.* Lett. 90, 057401 (2003).
- [18] C. L. Nehl, H. Liao, and J. H. Hafner, "Optical Properties of Star-Shaped Gold Nanoparticles," *Nano Lett.* 6, 683-688 (2006).
- [19] L. J. Sherry, R. Jin, C. A. Mirkin, G. C. Schatz, and R. P. VanDuyne, "Localized Surface Plasmon Resonance Spectroscopy of Single Silver Triangular Nanoprisms," *Nano Lett.* 6, 2060-2065 (2006).
- [20] H. Wang, D. W. Brandl, F. Le, P. Nordlander, "Nanorice: A Hybrid Plasmonic Nanostructure," *Nano Lett.* 6, 827-832 (2006).

